## Project selection problem:

- Set P of possible projects. Project v has an associated profit  $p_v$  (can be positive or negative).
- Some projects have requirements (taking course EA2 requires course EA1).
- Dependencies are modelled in a graph. Edge (u, v) means "can't do project u without also doing project v."
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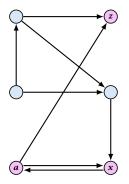
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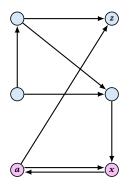
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## The prerequisite graph:

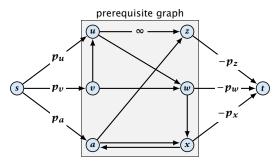
- $\{x, a, z\}$  is a feasible subset.
- $\{x, a\}$  is infeasible.





### Mincut formulation:

- Edges in the prerequisite graph get infinite capacity.
- Add edge (s, v) with capacity  $p_v$  for nodes v with positive profit.
- Create edge (v,t) with capacity  $-p_v$  for nodes v with negative profit.



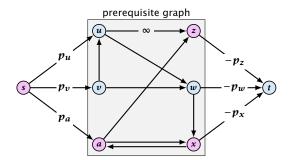


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### Proof.

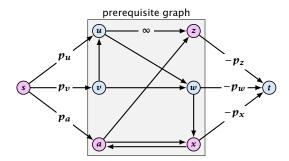
A is feasible because of capacity infinity edges.



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- ightharpoonup cap $(A, V \setminus A)$



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### Proof.

- ightharpoonup A is feasible because of capacity infinity edges.
- $v \in \bar{A}: p_v > 0$   $v \in \bar{A}: p_v < 0$ prerequisite graph  $p_u$

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- ► *A* is feasible because of capacity infinity edges.
- $v \in \bar{A}: p_v > 0$   $v \in A: p_v < 0$  $\sum_{v:p_v>0} p_v - \sum_{v\in A} p_v$ prerequisite graph  $p_u$